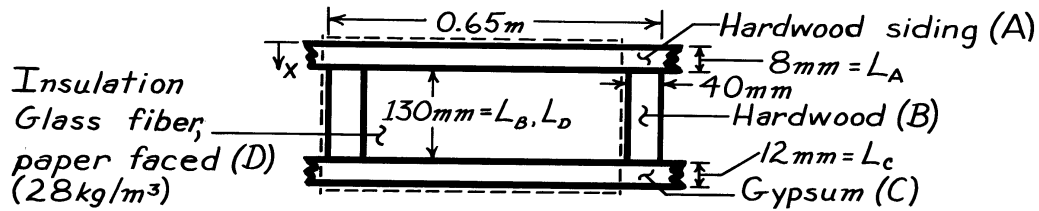


PROBLEM 3.15

KNOWN: Dimensions and materials associated with a composite wall (2.5m × 6.5m, 10 studs each 2.5m high).

FIND: Wall thermal resistance.

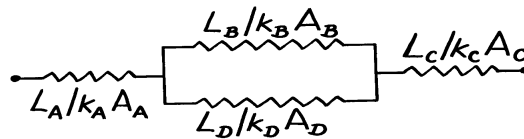
SCHEMATIC:



ASSUMPTIONS: (1) Steady-state conditions, (2) Temperature of composite depends only on x (surfaces normal to x are isothermal), (3) Constant properties, (4) Negligible contact resistance.

PROPERTIES: Table A-3 ($T \approx 300\text{K}$): Hardwood siding, $k_A = 0.094 \text{ W/m}\cdot\text{K}$; Hardwood, $k_B = 0.16 \text{ W/m}\cdot\text{K}$; Gypsum, $k_C = 0.17 \text{ W/m}\cdot\text{K}$; Insulation (glass fiber paper faced, 28 kg/m^3), $k_D = 0.038 \text{ W/m}\cdot\text{K}$.

ANALYSIS: Using the isothermal surface assumption, the thermal circuit associated with a single unit (enclosed by dashed lines) of the wall is



$$(L_A / k_A A_A) = \frac{0.008\text{m}}{0.094 \text{ W/m}\cdot\text{K} (0.65\text{m} \times 2.5\text{m})} = 0.0524 \text{ K/W}$$

$$(L_B / k_B A_B) = \frac{0.13\text{m}}{0.16 \text{ W/m}\cdot\text{K} (0.04\text{m} \times 2.5\text{m})} = 8.125 \text{ K/W}$$

$$(L_D / k_D A_D) = \frac{0.13\text{m}}{0.038 \text{ W/m}\cdot\text{K} (0.61\text{m} \times 2.5\text{m})} = 2.243 \text{ K/W}$$

$$(L_C / k_C A_C) = \frac{0.012\text{m}}{0.17 \text{ W/m}\cdot\text{K} (0.65\text{m} \times 2.5\text{m})} = 0.0434 \text{ K/W}.$$

The equivalent resistance of the core is

$$R_{eq} = (1/R_B + 1/R_D)^{-1} = (1/8.125 + 1/2.243)^{-1} = 1.758 \text{ K/W}$$

and the total unit resistance is

$$R_{tot,1} = R_A + R_{eq} + R_C = 1.854 \text{ K/W}.$$

With 10 such units in parallel, the total wall resistance is

$$R_{tot} = (10 \times 1/R_{tot,1})^{-1} = 0.1854 \text{ K/W}.$$

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COMMENTS: If surfaces parallel to the heat flow direction are assumed adiabatic, the thermal circuit and the value of R_{tot} will differ.