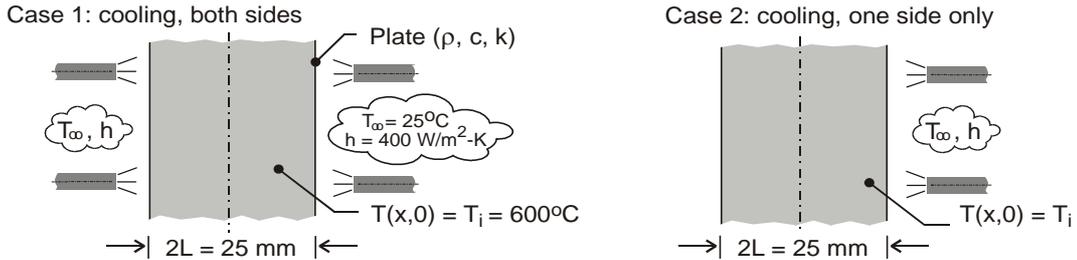


PROBLEM 5.54

KNOWN: Plate of thickness $2L = 25 \text{ mm}$ at a uniform temperature of 600°C is removed from a hot pressing operation. Case 1, cooled on both sides; case 2, cooled on one side only.

FIND: (a) Calculate and plot on one graph the temperature histories for cases 1 and 2 for a 500-second cooling period; use the *IHT* software; Compare times required for the maximum temperature in the plate to reach 100°C ; and (b) For both cases, calculate and plot on one graph, the variation with time of the maximum temperature difference in the plate; Comment on the relative magnitudes of the temperature gradients within the plate as a function of time.

SCHEMATIC:



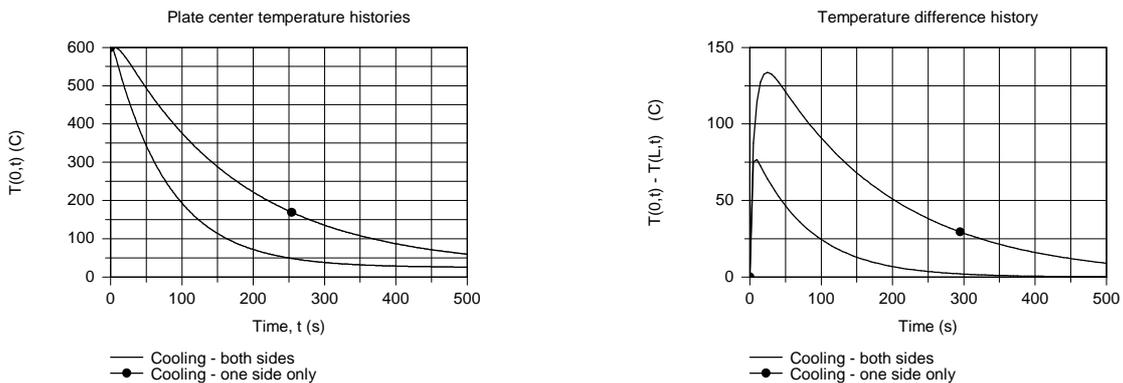
ASSUMPTIONS: (1) One-dimensional conduction in the plate, (2) Constant properties, and (3) For case 2, with cooling on one side only, the other side is adiabatic.

PROPERTIES: Plate (*given*): $\rho = 3000 \text{ kg/m}^3$, $c = 750 \text{ J/kg}\cdot\text{K}$, $k = 15 \text{ W/m}\cdot\text{K}$.

ANALYSIS: (a) From *IHT*, call up *Plane Wall, Transient Conduction* from the *Models* menu. For case 1, the plate thickness is 25 mm; for case 2, the plate thickness is 50 mm. The plate center ($x = 0$) temperature histories are shown in the graph below. The times required for the center temperatures to reach 100°C are

$$t_1 = 164 \text{ s} \qquad t_2 = 367 \text{ s} \qquad <$$

(b) The plot of $T(0, t) - T(L, t)$, which represents the maximum temperature difference in the plate during the cooling process, is shown below.



COMMENTS: (1) From the plate center-temperature history graph, note that it takes more than twice as long for the maximum temperature to reach 100°C with cooling on only one side.

(2) From the maximum temperature-difference graph, as expected, cooling from one side creates a larger maximum temperature difference during the cooling process. The effect could cause microstructure differences, which could adversely affect the mechanical properties within the plate.