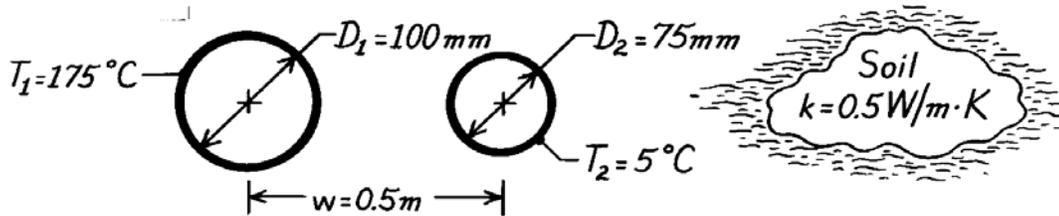


PROBLEM 4.14

KNOWN: Surface temperatures of two parallel pipe lines buried in soil.

FIND: Heat transfer per unit length between the pipe lines.

SCHEMATIC:



ASSUMPTIONS: (1) Steady-state conditions, (2) Two-dimensional conduction, (3) Constant properties, (4) Pipe lines are buried very deeply, approximating burial in an infinite medium, (5) Pipe length \$\gg D_1\$ or \$D_2\$ and \$w > D_1\$ or \$D_2\$.

ANALYSIS: The heat transfer rate per unit length from the hot pipe to the cool pipe is

$$q' = \frac{q}{L} = \frac{S}{L} k (T_1 - T_2).$$

The shape factor \$S\$ for this configuration is given in Table 4.1 as

$$S = \frac{2\pi L}{\cosh^{-1} \left[\frac{4w^2 - D_1^2 - D_2^2}{2D_1 D_2} \right]}.$$

Substituting numerical values,

$$\frac{S}{L} = 2\pi / \cosh^{-1} \left[\frac{4 \times (0.5\text{ m})^2 - (0.1\text{ m})^2 - (0.075\text{ m})^2}{2 \times 0.1\text{ m} \times 0.075\text{ m}} \right] = 2\pi / \cosh^{-1}(65.63)$$

$$\frac{S}{L} = 2\pi / 4.88 = 1.29.$$

Hence, the heat rate per unit length is

$$q' = 1.29 \times 0.5\text{ W/m}\cdot\text{K} (175 - 5)^\circ\text{C} = 110\text{ W/m.} \quad <$$

COMMENTS: The heat gain to the cooler pipe line will be larger than 110 W/m if the soil temperature is greater than \$5^\circ\text{C}\$. How would you estimate the heat gain if the soil were at \$25^\circ\text{C}\$?