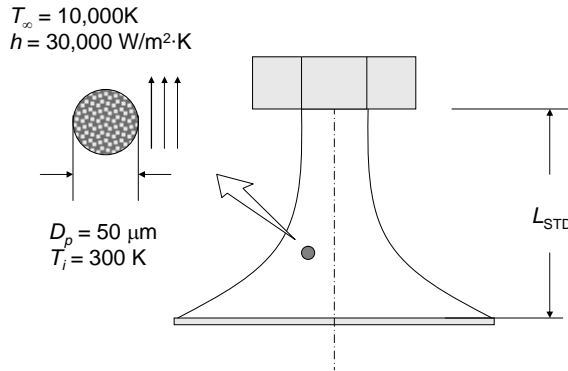


PROBLEM 5.26

KNOWN: Diameter and initial temperature of nanostructured ceramic particle. Plasma temperature and convection heat transfer coefficient. Properties and velocity of particles.

FIND: (a) Time-in-flight corresponding to 30% of the particle mass being melted. (b) Time-in-flight corresponding to the particle being 70% melted. (c) Standoff distances between the nozzle and the substrate associated with parts (a) and (b).

SCHEMATIC:



ASSUMPTIONS: (1) Constant properties. (2) Negligible radiation.

PROPERTIES: Given; $k = 5 \text{ W/m}\cdot\text{K}$, $\rho = 3800 \text{ kg/m}^3$, $c_p = 1560 \text{ J/kg}\cdot\text{K}$, $h_{sf} = 3577 \text{ kJ/kg}$, $T_{mp} = 2318 \text{ K}$.

ANALYSIS: (a) To determine whether the lumped capacitance assumption is appropriate, the Biot number is calculated as

$$Bi = \frac{h(r_o/3)}{k} = \frac{hD}{6k} = \frac{30,000 \text{ W/m}^2 \cdot \text{K} \times 50 \times 10^{-6} \text{ m}}{6 \times 5 \text{ W/m} \cdot \text{K}} = 0.05$$

Since $Bi < 0.1$, the lumped capacitance approximation is valid. The particle heating process can be divided into two stages.

Stage 1: Heating to the melting temperature. The time-of-flight for the first stage is found from Equation 5.5.

$$\begin{aligned} t_1 &= \frac{\rho V c}{h A_s} \ln \frac{\theta_i}{\theta} = \frac{\rho D c}{6 h} \ln \frac{T_i - T_\infty}{T_{mp} - T_\infty} \\ &= \frac{3800 \text{ kg/m}^3 \times 50 \times 10^{-6} \text{ m} \times 1560 \text{ J/kg} \cdot \text{K}}{6 \times 30,000 \text{ W/m}^2 \cdot \text{K}} \ln \frac{300 \text{ K} - 10,000 \text{ K}}{2318 \text{ K} - 10,000 \text{ K}} \\ &= 0.00038 \text{ s} \end{aligned}$$

Stage 2: Melting to 30% liquid. The second stage involves heat transfer to the particle which is isothermal at its melting point temperature. Hence

Continued...

PROBLEM 5.26 (Cont.)

$$t_{2,0.3} = \frac{\Delta E}{q} = \frac{0.3\rho V h_{sf}}{h A_s (T_\infty - T_{mp})} = \frac{0.05\rho D h_{sf}}{h (T_\infty - T_{mp})}$$

$$= \frac{0.05 \times 3800 \text{ kg/m}^3 \times 50 \times 10^{-6} \text{ m} \times 3577 \times 10^3 \text{ J/kg}}{30,000 \text{ W/m}^2 \cdot \text{K} \times (10,000 - 2318) \text{ K}} = 0.00015 \text{ s}$$

Therefore the required time-of-flight is $t_{\text{tot},0.3} = t_1 + t_{2,0.3} = 0.00038 \text{ s} + 0.00015 \text{ s} = 0.00053 \text{ s}$ <

(b) The calculation for the second stage may be repeated for 70% liquid, yielding $t_{2,0.7} = 0.00034 \text{ s}$.
Therefore the required time-of-flight is $t_{\text{tot},0.7} = t_1 + t_{2,0.7} = 0.00038 \text{ s} + 0.000341 \text{ s} = 0.00072 \text{ s}$ <

(c) The required standoff distances are

$$L_{\text{STD},0.3} = V t_{\text{tot},0.3} = 35 \text{ m/s} \times 0.00053 \text{ s} = 0.019 \text{ m} = 19 \text{ mm} <$$

$$L_{\text{STD},0.7} = V t_{\text{tot},0.7} = 35 \text{ m/s} \times 0.00072 \text{ s} = 0.025 \text{ m} = 25 \text{ mm}$$

COMMENTS: (1) Assuming the particles to have an emissivity of $\varepsilon_p = 0.4$ and radiation is exchanged with surroundings at an assumed temperature of $T_{\text{sur}} = 300 \text{ K}$, the radiation heat transfer coefficient may be found from Equation 1.9 as

$$h_r = \varepsilon_p \sigma (T_{\text{mp}} + T_{\text{sur}})(T_{\text{mp}}^2 + T_{\text{sur}}^2) = 0.4 \times 5.67 \times 10^{-8} \frac{\text{W}}{\text{m}^2 \cdot \text{K}^4} (2318 + 300) \text{ K} \times (2318^2 + 300^2) = 320 \text{ W/m}^2 \cdot \text{K}.$$

Hence $h_r \ll h_{\text{conv}}$ and radiation heat transfer is negligible. (2) To deliver a partially-molten droplet to the substrate, standoff distances on the order of 20 mm need to be maintained. This is a reasonable requirement. (3) See I. Ahmed and T.L. Bergman, “Simulation of Thermal Plasma Spraying of Partially Molten Ceramics: Effect of Carrier Gas on Particle Deposition and Phase Change Phenomena,” *ASME Journal of Heat Transfer*, vol. 123, pp. 188-196, 2001, for more information.