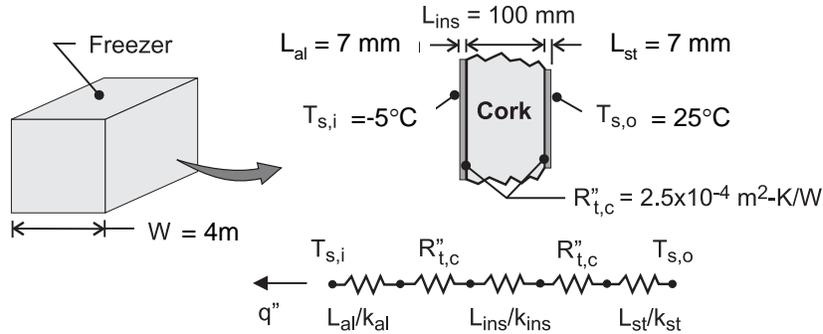


PROBLEM 3.31

KNOWN: Size and surface temperatures of a cubical freezer. Materials, thicknesses and interface resistances of freezer wall.

FIND: Cooling load.

SCHEMATIC:



ASSUMPTIONS: (1) Steady-state, (2) One-dimensional conduction, (3) Constant properties.

PROPERTIES: Table A-1, Aluminum 2024 (~267K): $k_{al} = 173 \text{ W/m}\cdot\text{K}$. Table A-1, Carbon steel AISI 1010 (~295K): $k_{st} = 64 \text{ W/m}\cdot\text{K}$. Table A-3 (~300K): $k_{ins} = 0.039 \text{ W/m}\cdot\text{K}$.

ANALYSIS: For a unit wall surface area, the total thermal resistance of the composite wall is

$$R''_{tot} = \frac{L_{al}}{k_{al}} + R''_{t,c} + \frac{L_{ins}}{k_{ins}} + R''_{t,c} + \frac{L_{st}}{k_{st}}$$

$$R''_{tot} = \frac{0.007\text{m}}{173 \text{ W/m}\cdot\text{K}} + 2.5 \times 10^{-4} \frac{\text{m}^2 \cdot \text{K}}{\text{W}} + \frac{0.100\text{m}}{0.039 \text{ W/m}\cdot\text{K}} + 2.5 \times 10^{-4} \frac{\text{m}^2 \cdot \text{K}}{\text{W}} + \frac{0.007\text{m}}{64 \text{ W/m}\cdot\text{K}}$$

$$R''_{tot} = (4.0 \times 10^{-5} + 2.5 \times 10^{-4} + 2.56 + 2.5 \times 10^{-4} + 10.9 \times 10^{-5}) \text{m}^2 \cdot \text{K} / \text{W} = 2.56 \text{ m}^2 \cdot \text{K} / \text{W}$$

Hence, the heat flux is

$$q'' = \frac{T_{s,o} - T_{s,i}}{R''_{tot}} = \frac{[25 - (-5)]^\circ\text{C}}{2.56 \text{ m}^2 \cdot \text{K} / \text{W}} = 11.7 \frac{\text{W}}{\text{m}^2}$$

and the cooling load is

$$q = A_s q'' = 6 \text{ W}^2 q'' = 96 \text{ m}^2 \times 11.7 \text{ W/m}^2 = 1123 \text{ W} \quad <$$

COMMENT: Thermal resistances associated with the cladding and the adhesive joints are negligible compared to that of the insulation.