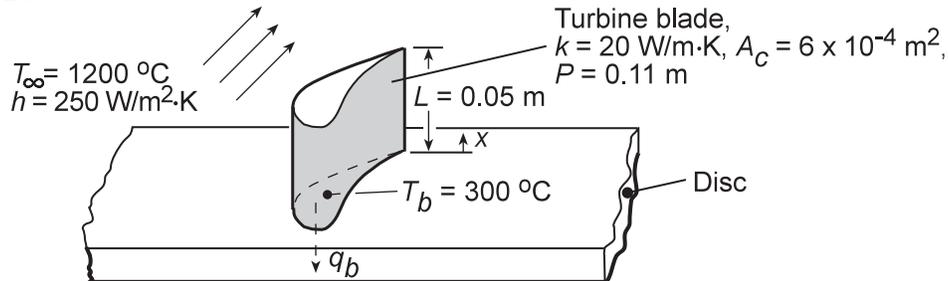


PROBLEM 3.126

KNOWN: Dimensions and thermal conductivity of a gas turbine blade. Temperature and convection coefficient of gas stream. Temperature of blade base and maximum allowable blade temperature.

FIND: (a) Whether blade operating conditions are acceptable, (b) Heat transfer to blade coolant.

SCHEMATIC:



ASSUMPTIONS: (1) One-dimensional, steady-state conduction in blade, (2) Constant k , (3) Adiabatic blade tip, (4) Negligible radiation.

ANALYSIS: Conditions in the blade are determined by Case B of Table 3.4.

(a) With the maximum temperature existing at $x = L$, Eq. 3.80 yields

$$\frac{T(L) - T_{\infty}}{T_b - T_{\infty}} = \frac{1}{\cosh mL}$$

$$m = (hP/kA_c)^{1/2} = \left(250 \text{ W/m}^2 \cdot \text{K} \times 0.11 \text{ m} / 20 \text{ W/m} \cdot \text{K} \times 6 \times 10^{-4} \text{ m}^2\right)^{1/2}$$

$$m = 47.87 \text{ m}^{-1} \quad \text{and} \quad mL = 47.87 \text{ m}^{-1} \times 0.05 \text{ m} = 2.39$$

From Table B.1, $\cosh mL = 5.51$. Hence,

$$T(L) = 1200^\circ \text{C} + (300 - 1200)^\circ \text{C} / 5.51 = 1037^\circ \text{C} \quad <$$

and the operating conditions are acceptable.

(b) With $M = (hPkA_c)^{1/2} \Theta_b = \left(250 \text{ W/m}^2 \cdot \text{K} \times 0.11 \text{ m} \times 20 \text{ W/m} \cdot \text{K} \times 6 \times 10^{-4} \text{ m}^2\right)^{1/2} (-900^\circ \text{C}) = -517 \text{ W}$, Eq. 3.81 and Table B.1 yield

$$q_f = M \tanh mL = -517 \text{ W} (0.983) = -508 \text{ W}$$

Hence, $q_b = -q_f = 508 \text{ W} \quad <$

COMMENTS: Radiation losses from the blade surface and convection from the tip will contribute to reducing the blade temperatures.