

PROBLEM 6.42

KNOWN: Form of Nusselt number for flow of air or a dielectric liquid over components of a circuit card.

FIND: Ratios of time constants associated with intermittent heating and cooling. Fluid that provides faster thermal response.

PROPERTIES: Prescribed. Air: $k = 0.026 \text{ W/m}\cdot\text{K}$, $\nu = 2 \times 10^{-5} \text{ m}^2/\text{s}$, $\text{Pr} = 0.71$. Dielectric liquid: $k = 0.064 \text{ W/m}\cdot\text{K}$, $\nu = 10^{-6} \text{ m}^2/\text{s}$, $\text{Pr} = 25$.

ANALYSIS: From Eq. 5.7, the thermal time constant is

$$\tau_t = \frac{\rho \nabla c}{\bar{h} A_s}$$

Since the only variable that changes with the fluid is the convection coefficient, where

$$\bar{h} = \frac{k}{L} \overline{\text{Nu}}_L = \frac{k}{L} C \text{Re}_L^m \text{Pr}^n = \frac{k}{L} C \left(\frac{VL}{\nu} \right)^m \text{Pr}^n$$

the desired ratio reduces to

$$\frac{\tau_{t,\text{air(a)}}}{\tau_{t,\text{dielectric(d)}}} = \frac{\bar{h}_d}{\bar{h}_a} = \frac{k_d}{k_a} \left(\frac{\nu_a}{\nu_d} \right)^m \left(\frac{\text{Pr}_d}{\text{Pr}_a} \right)^n$$

$$\frac{\tau_{t,a}}{\tau_{t,d}} = \frac{0.064}{0.026} \left(\frac{2 \times 10^{-5}}{10^{-6}} \right)^{0.8} \left(\frac{25}{0.71} \right)^{0.33} = 88.6$$

Since its time constant is nearly two orders of magnitude smaller than that of the air, the dielectric liquid is clearly the fluid of choice. <

COMMENTS: The accelerated testing procedure suggested by this problem is commonly used to test the durability of electronic packages.