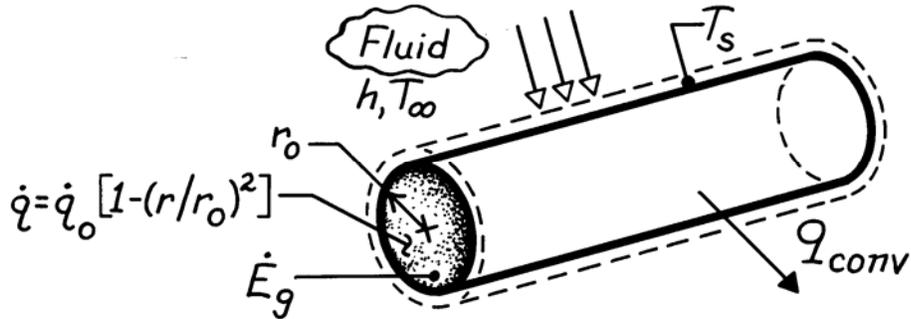


### PROBLEM 1.44

**KNOWN:** Radial distribution of heat dissipation in a cylindrical container of radioactive wastes. Surface convection conditions.

**FIND:** Total energy generation rate and surface temperature.

**SCHEMATIC:**



**ASSUMPTIONS:** (1) Steady-state conditions, (2) Negligible temperature drop across thin container wall.

**ANALYSIS:** The rate of energy generation is

$$\begin{aligned}\dot{E}_g &= \int \dot{q} dV = \dot{q}_o \int_0^{r_o} [1 - (r/r_o)^2] 2\pi r L dr \\ \dot{E}_g &= 2\pi L \dot{q}_o \left( r_o^2 / 2 - r_o^2 / 4 \right)\end{aligned}$$

or per unit length,

$$\dot{E}'_g = \frac{\pi \dot{q}_o r_o^2}{2} \quad <$$

Performing an energy balance for a control surface about the container yields, at an instant,

$$\dot{E}'_g - \dot{E}'_{out} = 0$$

and substituting for the convection heat rate per unit length,

$$\begin{aligned}\frac{\pi \dot{q}_o r_o^2}{2} &= h(2\pi r_o)(T_s - T_\infty) \\ T_s &= T_\infty + \frac{\dot{q}_o r_o}{4h} \quad <\end{aligned}$$

**COMMENTS:** The temperature within the radioactive wastes increases with decreasing  $r$  from  $T_s$  at  $r_o$  to a maximum value at the centerline.